



**CBCS CURRICULUM OF
P.G. MATHEMATICS PROGRAMME**

SUBJECT CODE = MATH

FOR POST GRADUATE COURSES UNDER NILAMBER PITAMBER UNIVERSITY

Members of Board of Studies of CBCS Post-Graduate Syllabus as per
Guidelines of the Nilamber-Pitamber University, Medininagar.

Meeting of Board of Study

Department of Mathematics, NPU

Medininagar, Jharkhand

On line meeting of Board of Study held on 19/03/2021 in the Department of Mathematics, NPU, Medininagar, Palamu, Jharkhand at 3:00 PM to 4:30 PM Under Chairmanship of Dr. Gajendra Singh, Department of Mathematics, NPU. The following members and external expert prof. Dr. Rajendra Prasad, Dept. of Mathematics, Lucknow University, Lucknow, UP, India have attended in the meeting:

1. Dr. Gajendra Singh (Chairman)

G.Singh

2. Prof. Dr. Rajendra Prasad (External Expert)

rpasad
19/03/2021

3. Dr. Uday Kumar (Member)

Uday
19.03.21
Dr. Uday Kumar

4. Dr. R.B. Azad (Member)

R.B. Azad
19.3.21
Dr. Rami Bilas Azad

5. Dr. Ravishanker (Member)

Ravishanker

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COURSE STRUCTURE FOR M.A./M.Sc. MATHEMATICS

Semester	Courses	Paper	Paper Code	Credit	Hrs./week
I	Foundation Course	FC	FCMATH101	5	5 (L)+1(T)
	Core Course	CC1	CCMATH101	5	5 (L)+1(T)
	Core Course	CC2	CCMATH102	5	5 (L)+1(T)
	Core Course	CC3	CCMATH103	5	5 (L)+1(T)
II	Ability Enhancement Course	EC1	ECMATH201	5	5 (L)+1(T)
	Core Course	CC4	CCMATH204	5	5 (L)+1(T)
	Core Course	CC5	CCMATH205	5	5 (L)+1(T)
	Practicals on Core Course	CC6-P	CCMATH206	5	10
III	Core Course	CC7	CCMATH307	5	5 (L)+1(T)
	Core Course	CC8	CCMATH308	5	5 (L)+1(T)
	Elective (GE/DC)	EC2	ECMATH302	5	5 (L)+1(T)
	Elective (GE/DC)	EC3	ECMATH303	5	5 (L)+1(T)
IV	Core Course	CC9	CCMATH409	5	5 (L)+1(T)
	Elective (GE/DC)	EC4	ECMATH404	5	5 (L)+1(T)
	Elective (GE/DC)	EC5	ECMATH405	5	5 (L)+1(T)
	Project/Dissertation	CC10	CCMATH410	5	10

Table AI-2.1 Semester wise Examination Structure for Mid Sem & End Sem Examinations:

Sem				Core, SE/GE/DC & Compulsory FC Courses	Examination Structure		
	Paper	Paper Code	Credit	Name of Paper	Mid Semester Evaluation (F.M.)	End Semester Evaluation (F.M.)	End Semester Practical/ Viva (F.M.)
I	FC	FCMATH101	5	Foundation Course	30	70	----
	CC1	CCMATH101	5	Real Analysis	30	70	----
	CC2	CCMATH102	5	Topology	30	70	----
	CC3	CCMATH103	5	Complex Analysis	30	70	----
II	EC1	ECMATH201	5	Programming in C & Matlab	30	70	----
	CC4	CCMATH204	5	Ordinary Differential Equation	30	70	----
	CC5	CCMATH205	5	Defferential Geometry and Tensor Analysis	30	70	----
	CC6-P	CCMATH206P	5	Programming in C & Matlab-PR	----	----	100
III	CC7	CCMATH307	5	Functional Analysis	30	70	----
	CC8	CCMATH308	5	Partial Differential Equation	30	70	----
	EC2	ECMATH302	5	A. Optimization Techniques	30	70	----
				B. Advance Discrete Mathematics			
				C. Integral Transforms			
	EC3	ECMATH303	5	A. Fluid Dynamics	30	70	----
				B. Analytical Dynamics and Calculus of Variations			
				C. Probability and Statistics			
IV	CC9	CCMATH409	5	Numerical Solution of ODE/PDE	30	70	----
	EC4	ECMATH404	5	A. Operations Research	30	70	
				B. Fourier and Wavelet Analysis			
				C. Mathematical Modeling			
	EC5	ECMATH405	5	A. Integral Equations	30	70	----
				B. Hadamard Matrices and Combinatorial Designs			
				C. Mathematics of Finance and Insurance			
CC10	CCMATH410	5	Project	----	----	100	

UNIVERSITY DEPARTMENT OF MATHETMATICS, N.P. UNIVERSITY
CBCS PATTERN SYLLABUS

M.Sc./M.A. MATHEMATICS
SYLLABUS BASED ON CBCS SEMESTER SYSTEM

SEMESTER I



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Marks 30 (MSE 20 1 Hr + 5 Attd. + 5 Assign) + 70 (ESE : 3 Hrs) = 100

Pass Marks (MSE : 17 + ESE : 28) = 45

MID SEMESTER EXAMINATION (MSE)

The Mid Semester Examination shall have three components: **(a)** Two Semester Internal Assessment Test **(SIA)** of 20 marks each. “Better of Two” shall be applicable for computation of marks for SIA. **(b)** Attendance / Regular Interactions of 05 marks and **(c)** Assignment of 05 marks.

END SEMESTER EXAMINATION (ESE)

A total of **EIGHT** questions will be set in which Question 1 will be **Short Answer Type** and **COMPULSORY**. Any **four** questions shall have to be answered by the examinees out of the remaining seven questions. The questions will be of equal marks and will be so framed that the students are able to answer them within the stipulated time.

Paper Code: FCMATH101

Foundation Course

Credits: 5, Full Marks: 70, Pass Marks: 28

Time: 3 hours

Unit I GROUP THEORY

Lectures – 20

Groups : Finite permutation groups S_n and A_n Normal and Subnormal series, Jordan-Holder theorem, Solvable groups, Nilpotent groups. Group action, orbit – stabilizer theorem, Sylow’s theorems (proofs using group actions).

Unit II LINEAR ALGEBRA

Lectures – 20

Matrix of a linear transformation, Canonical Forms – Similarity of linear transformations, Invariant subspaces, Eigen values and Eigen vectors, Reduction to diagonal, triangular and Jordan forms, The primary decomposition theorem.

Unit III Number Theory

Lectures – 20

Fundamental Theorem of Arithmetic, Properties of prime numbers, Euclid’s algorithm, HCF, LCM. Congruence, Linear Congruence, Chinese remainder theorem and applications, Euler’s function, Fermat’s little theorem, Wilson’s theorem.

Unit IV Real Analysis

Lectures – 15

Sequence of real numbers, monotonic, bounded sequence, limit of the sequence, Cauchy’s general principle of convergence for sequence. Infinite series of real numbers, Cauchy’s general principle of convergence of series. Auxiliary series, Tests of convergence. Alternating Series, Leibnitz test, absolutely convergence series, Conditionally convergent series.

Text/ Reference Books:

1. D.S. Dummit, R.M. Foote, Abstract Algebra – John Wiley & Sons (2013)
2. J.N. Herstein. Topics in Algebra, Wiley Eastern Ltd. , New Delhi, 1975
3. K. Hoffman and R. Kunze (2nd edition), Linear Algebra, Prentice Hall of India, New Delhi (1997)
4. W Rudin, Principles of Mathematical Analysis, Mc-Graw Hill, 3rd Edition
5. Hardy and Wright, An Introduction to Theory of Numbers, Oxford Univ. Press, Sixth Edition.

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END SEMESTER EXAMINATION (ESE)

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Paper Code: CCMATH101

Real Analysis Credits: 5, Full Marks: 70, Pass Marks: 28

Time: 3 hours

Unit I – UNIFORM CONVERGENCE

Lectures – 20

Sequences and series of functions, pointwise and uniform convergence. Cauchy criterion for uniform convergence, Weierstrass M-test, Abel's and Dirichlet's test for uniform convergence, uniform convergence and continuity, preservation of differentiability and integrability theorems.

[2 QUESTIONS]

Unit II – FUNCTIONS OF SEVERAL VARIABLES

Lectures – 20

Derivative of functions in an open subset of \mathbb{R}^n into \mathbb{R}^m as a linear transformation. Chain rule. Partial derivatives. Taylor's theorem. Inverse function theorem. Implicit function theorem, Jacobians.

[2 QUESTIONS]

Unit III - MEASURE

Lectures – 20

Motivation and Concept of Measure of a set, Outer measure, measurable sets, Lebesgue measures, A non-measurable set, measurable functions, Littlewood's three principles.

[2 QUESTIONS]

Unit IV – The Lebesgue integral

Lectures – 15

Lebesgue integral of a bounded function over a finite measure, The integral of a non-negative function, The general Lebesgue integral, Convergence theorems, Convergence in measure.

[2 QUESTIONS]

Text/ Reference Books:

1. Walter Rudin, Principles of Mathematical Analysis, 3rd ed. McGraw-Hill
2. T.M. Apostol, Mathematical Analysis, Narosa Publ., New Delhi, 1985.
3. R. G. Bartle and Donald R Sherbert, Real Analysis, John Wiley & Sons, 4th Edition
4. H. L. Royden, Real Analysis, McMillan, 4th Edition

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END SEMESTER EXAMINATION (ESE)

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Paper Code: CCMATH102

Topology

Credits: 5, Full Marks: 70, Pass Marks: 28

Time: 3 hours

UNIT I – Fundamentals of a topological space

Lectures – 20

Definition and examples of topological spaces. Closed sets, closure. Dense subsets. Neighborhoods, Interior, exterior and boundary. Accumulation points and derived sets. Bases and sub-bases. Subspaces and relative topologies. Quotient topology.

[2 QUESTIONS]

UNIT II – Continuity and connectedness

Lectures – 20

Continuity and homeomorphism, Product of topological spaces, connected space and its properties.

[2 QUESTIONS]

UNIT III – Countability and separation axiom

Lectures – 20

First and second countable spaces. Lindelof's theorem, separable spaces, second countability and separability. Separation axioms T_0, T_1, T_2, T_3, T_4 : their characterizations and basic properties. Urysohn's Lemma. Tietze extension theorem.

[2 QUESTIONS]

UNIT IV – Compactness

Lectures – 15

Compactness, continuous image of compact sets. Basic property of compactness. Compactness and finite intersection property Tychonoff's theorem, one point compactification of a topological space.

[2 QUESTIONS]

Text/ Reference Books:

1. K.D. Joshi. Introduction to General Topology, Wiley Eastern Ltd. 1983.
2. W.J. Pervin. Foundations of General Topology Academic Press Inc. New York 1964.
3. G.F. Simmons, Introduction to Topology and Modern Analysis, Mc Graw Hill Int. book company.
4. J.R. Munkres, Topology A first course, Prentice hall India Pvt. Ltd.
5. S. Lipschutz, General Topology, Schaum's out line series.

UNIVERSITY DEPARTMENT OF MATHEMATICS, N.P. UNIVERSITY**CBCS PATTERN SYLLABUS****Marks 30 (MSE 20 1 Hr + 5 Attd. + 5 Assign) + 70 (ESE : 3 Hrs) = 100****Pass Marks (MSE : 17 + ESE : 28) = 45****MID SEMESTER EXAMINATION (MSE)**

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Paper Code: CCMATH103**Complex Analysis****Credits: 5, Full Marks: 70, Pass Marks: 28****Time: 3 hours****UNIT I – Complex Integration**

Cauchy-Goursat Theorem, Cauchy's Integral formula, Higher order derivatives, Morera's Theorem, Cauchy's inequality, Liouville's theorem and Fundamental theorem of Algebra.

Lectures – 20

[2 QUESTIONS]

UNIT II – Power Series

Circle of convergence. Absolute and uniform convergence. Taylor's theorem, Laurent's theorem. Maximum modulus principle.

Lectures – 20

[2 QUESTIONS]

UNIT III – Singularities and Cauchy Residue Theorem

Isolated singularities. Meromorphic functions. The argument principle, Rouché's theorem poles and Zeros. Residues, Cauchy's residue theorem. Contour Integration. Evaluation of integrals.

Lectures – 20

[2 QUESTIONS]

UNIT IV – Analytic Continuation and its application

Definition of Analytic continuations and related problems, Uniqueness theorem of Analytic continuation, Standard method/Power series method of Analytic continuation along a curve, Singularity of the circle of convergence of power series.

Lectures – 15

[2 QUESTIONS]

Text/ Reference Books:

1. Churchill and Brown, Complex variables and applications, McGraw-Hill Pub. Company.
2. Walter Rudin. Real and Complex Analysis. Mc Graw Hill Book Co. 1966
3. E.C. Titchmarsh. The theory of Functions. Oxford University Press. London.

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Paper Code: ECMATH201

Programming in C and MATLAB

Credits: 5, Full Marks: 70, Pass Marks: 28

Time: 3 hours

UNIT -I

Lectures – 20

Planning the Computer Program : Concept of problem solving, Problem definition, Program design, Debugging, Types of errors in programming, Documentation. Techniques of Problem Solving : Flowcharting, algorithms, pseudo code, decision table, Structured programming concepts, Programming methodologies viz. top-down and bottom-up programming.

Overview of C : History of C, Importance of C, Structure of a C Program.

Elements of C : C Character set, identifiers and keywords, Data types, Constants and Variables, Assignment statement, Symbolic constant.

Input/output : Unformatted & formatted I/O function, Input functions viz. scanf (), getch (), getche (), getchar (), gets (), output functions viz. printf (), putchar (), puts (). Operators & Expression : Arithmetic, relational, logical, bitwise, unary, assignment, conditional operators and special operators. Arithmetic expressions, evaluation of arithmetic expression, type casting and conversion, operator hierarchy & associativity.

Decision making & branching : Decision making with IF statement, IF-ELSE statement, Nested IF statement, ELSE-IF ladder, switch statement, goto statement.

Decision making & looping : For, while, and do-while loop, jumps in loops, break, continue statement. Understanding header files : stdio.h, math.h, ctype.h and its function prototypes.

[2 QUESTIONS]

UNIT II –

Lectures – 20

Functions : Definition, prototype, passing parameters, recursion.

Storage classes in C : auto, extern, register and static storage class, their scope, storage & lifetime.

Structure, Union, enum

Arrays : Definition, types, initialization, processing an array, Strings & arrays.

Pointer and its implementation using Function, Structure, Union, Array

File Handling : Needs of File Handling, File Modes, Type of Files, Open/Create, Read, Write, Delete, Copy, Rename, searching etc.

[2 QUESTIONS]

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UNIT III –

Lectures – 20

Introduction to MATLAB, Elementary MATH Built-in-Functions, Creating Arrays, one dimensional, two dimensional arrays, variable, strings. Mathematical operations with arrays, Script files, Two dimensional plots, Functions and Function files.

[2 QUESTIONS]

UNIT IV –

Lectures – 15

Programming in MATLAB, Relational and Logical operators, Conditional statements, the switch-case statement, Loops, Nested Loops and Nested conditional statements, The break and continue commands, Polynomials, Curve Fitting and Interpolation, Applications to Numerical Analysis.

[2 QUESTIONS]

Text/ Reference Books:

1. Yashwant Kanetker, Working with C. BPB
2. Reema Tharej, Programming with C, Oxford
3. Balagurusamy, E., Computing Fundamentals and C Programming, Tata McGraw-Hill
4. Jeri R. Hanly & Elliot P. Koffman, Problem Solving and Program Design in C, Addison Wesley.
5. Yashwant Kanetker, Let us C, BPB
6. Rajaraman, V., Computer Programming in C, PHI
7. Amos Gilat, MATLAB- An introduction with Applicatins, Wiley India

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Paper Code: CCMATH204

Ordinary Differential Equations

Credits: 5, Full Marks: 70, Pass Marks: 28

Time: 3 hours

UNIT I – First order ODE

Lectures – 20

Existence and uniqueness of the solution to ODE, Picard's existence theorem, Lipschitz condition, Uniqueness theorem, Picard's method of successive approximation.

[2 QUESTIONS]

UNIT II – Second and higher order ODE

Lectures – 20

Algebraic properties of solutions of homogeneous equations & wronskian of second order ODE, nth order ODE, Wronskian or n functions and its properties, Annihilator method to solve non homogeneous ODE with constant coefficients, initial value problem, Existence and uniqueness theorem.

[2 QUESTIONS]

UNIT III – Linear System of ODE's

Lectures – 20

Linear system of ODEs, Existence and Uniqueness of linear system, linear homogeneous system with constant coefficients, method of eigen value and eigen vectors, Fundamental solution, Reduction of higher order linear equation into first order linear equations.

[2 QUESTIONS]

UNIT IV – Boundary Value Problem

Lectures – 15

Sturm-Liouville boundary value problem with homogeneous boundary conditions. Green's function, Green's function techniques for solving self-adjoint boundary value problem.

[2 QUESTIONS]

Text/ Reference Books:

1. E.A. Coddington and N. Levinson. Theory of Ordinary Differential Equations. Mc Graw-Hill, NY (1955).
2. M. Brawn, Differential equations and their applications, Springer-Verlag New York (1992).
3. Chakrabarti, Elements of ordinary differential equations and special functions, New Age, Int. Publ. (1990).
4. M.D. Raisinghani, Advanced differential equations, S. Chand and Company, 2001
5. A Coddington, An introduction to Ordinary Differential equations, Prentice Hall of India, New delhi, 1987.

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END SEMESTER EXAMINATION (ESE)

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Paper Code: CCMATH205

Differential Geometry and Tensor Analysis

Credits: 5, Full Marks: 70, Pass Marks: 28

Time: 3 hours

UNIT I – Curves in Space

Curvature and torsion. Serret-Frenet formula. Circular helix, the circle of curvature. Osculating sphere, Bertrand curves.
[2 QUESTIONS]

Lectures – 20

UNIT II – Curves on a Surface

Curves on a surface-parametric curves. Fundamental magnitude, curvature of normal section. Principal directions and principal curvatures, lines of curvature, Rodrique's formula. Dupin's theorem, theorem of Euler, Conjugate directions and Asymptotic lines.
[2 QUESTIONS]

Lectures – 20

UNIT III – Family of Surfaces

One parameter family of surfaces – Envelope the edge of regression, Developables associated with space curves. Gaussian Curvature, Surface of constant curvature.
[2 QUESTIONS]

Lectures – 20

UNIT IV – Basics of tensor

Tensors, Tensor Algebra, Contraction, Quotient theorem. Metric Tensor, Angle between two vector.
[2 QUESTIONS]

Lectures – 15

Text/ Reference Books:

1. C.E. Weatherburn. Differential geometry of three dimensions.
2. C.E. Weatherburn. Tensor Calculus.
3. R.S. Mishra, Tensor Calculus and Riemannian Geometry.
4. T.J. Willmore, Differential Geometry.

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Paper Code: CCMATH206P

Programming in C & MATLAB (Practical)

Credits: 5, Full Marks: 70, Pass Marks: 28

Time: 3 hours

Programming in C :

Write programs to understand different logics using flow chart.

Write programs to understand printf, scanf, gets, getch, puts, sqrt etc functions.

Write programs to illustrate the concepts of constants, variables and data types.

Write programs to illustrate operators and expressions in C.

Write programs to illustrate decision making and branching in C.

Write programs to illustrate decision making and looping in C.

Analysis of various programs, i.e. Find the syntax error, logical error and outputs.

Write programs to illustrate array in C.

Write programs to illustrate of user defined functions.

Write programs to illustrate structure and unions.

Write programs to illustrate concept of pointers, character strings and string manipulations.

Write programs to illustrate of user defined functions using pointers, array, structure, union etc.

Write programs to illustrate File Handling in C.

Programming in MATLAB :

Write programs to illustrate Built-in functions and Arrays

Write Programs to illustrate Script files, functions and function files

Write programs to illustrate two dimensional plots

Write programs to illustrate curve fitting and interpolation.

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END SEMESTER EXAMINATION (ESE)

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Paper Code: CCMATH307

Functional Analysis

Credits: 5, Full Marks: 70, Pass Marks: 28

Time: 3 hours

UNIT I – Normed linear spaces

Lectures – 20

Normed Linear Spaces: Definition and Examples, NLS as a metric space, Open sets, closed sets etc in a NLS, Convergence and Continuity. Banach spaces and examples. Quotient space of normed linear spaces and its completeness, equivalent norms. [2 QUESTIONS]

UNIT II – Transformation on linear spaces

Lectures – 20

Bounded linear transformations, normed linear spaces of bounded linear transformations, dual spaces with examples. Hahn-Banach theorem Open mapping and closed graph theorem, the natural imbedding of N in N^{**} . Reflexive spaces. [2 QUESTIONS]

UNIT III – Hilbert Spaces

Lectures – 20

Inner product spaces. Hilbert spaces. Orthonormal Sets. Bessel's inequality. Complete orthonormal sets and Parseval's identity. Projection theorem. Riesz representation theorem Reflexivity of Hilbert spaces. [2 QUESTIONS]

UNIT IV – Operators in Hilbert Space

Lectures – 15

Linear Transformation & Linear Functionals. Adjoint of an operator on a Hilbert space.. Self-adjoint operators. Positive, normal and unitary operators. [2 QUESTIONS]

Text/ Reference Books:

1. G.F. Simmons, Topology and modern analysis TMH.
2. G. Bachman and L. Narici, Functional Analysis, A P.
3. R.E. Edwards, Functional Analysis. Holt Rinehart and Winston, New York 1958
4. C Goffman and G. Pedrick. First Course in Functional Analysis, PHT, 1987
5. Kreyszig, Functional analysis with applications, John Wiley and sons.

UNIVERSITY DEPARTMENT OF MATHEMATICS, N.P. UNIVERSITY
CBCS PATTERN SYLLABUS W.E.F. 2017-18

Marks 30 (MSE 20 1 Hr + 5 Attd. + 5 Assign) + 70 (ESE : 3 Hrs) = 100
Pass Marks (MSE : 17 + ESE : 28) = 45

MID SEMESTER EXAMINATION (MSE)

The Mid Semester Examination shall have three components: (a) Two Semester Internal Assessment Test (SIA) of 20 marks each. "Better of Two" shall be applicable for computation of marks for SIA. (b) Attendance / Regular Interactions of 05 marks and (c) Assignment of 05 marks.

END SEMESTER EXAMINATION (ESE)

A total of **EIGHT** questions will be set in which Question 1 will be **Short Answer Type** and **COMPULSORY**. Any **four** questions shall have to be answered by the examinees out of the remaining seven questions. The questions will be of equal marks and will be so framed that the students are able to answer them within the stipulated time.

Paper Code: CCMATH308

Partial Differential Equation

Credits: 5, Full Marks: 70, Pass Marks: 28

Time: 3 hours

UNIT I – Classification of 2nd order PDE & Laplace equation

Lectures – 20

Classification of second order PDE & reduction to Canonical forms, Fundamental Solutions of two dimensional Laplace equation in Cartesian form.

[2 QUESTIONS]

UNIT II – Heat Equation

Lectures – 20

Derivation and Fundamental solution of one dimensional Heat equation in Cartesian form. Application Problems.

[2 QUESTIONS]

UNIT III – Wave Equation

Lectures – 20

Derivation and Fundamental solution of one dimensional Wave equation in Cartesian form. Application Problems.

[2 QUESTIONS]

UNIT IV – Integral Transforms and Green's function Methods of Solution

Lectures – 15

Solutions of P.d.e. using separation of variables, Fourier transform and Laplace transform, Green's function and solutions of boundary value problems using Laplace transformation.

[2 QUESTIONS]

Text/ Reference Books:

1. L.C. Evans, Partial Differential Equations, Graduate Studies in Mathematics, Volume 19, AMS, 1998.
2. I.N. Sneddon, Use of integrals transforms, McGraw Hill.
3. P. Prasad and R. Ravindran, Partial differential equation.
4. K. Sankara Rao, Partial differential equation, new age.
5. E. Kreyszig, Advanced Engineering Mathematics, John Wiley & Sons.

UNIVERSITY DEPARTMENT OF MATHEMATICS, N.P. UNIVERSITY
CBCS PATTERN SYLLABUS W.E.F. 2017-18

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Pass Marks (MSE : 17 + ESE : 28) = 45

MID SEMESTER EXAMINATION (MSE)

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END SEMESTER EXAMINATION (ESE)

A total of **EIGHT** questions will be set in which Question 1 will be **Short Answer Type** and **COMPULSORY**. Any **four** questions shall have to be answered by the examinees out of the remaining seven questions. The questions will be of equal marks and will be so framed that the students are able to answer them within the stipulated time.

Paper Code: ECMATH302

Students should opt for anyone of the following three courses :

- A. **OPTIMIZATION TECHNIQUES**
- B. **ADVANCED DISCRETE MATHEMATICS**
- C. **INTEGRAL TRANSFORMS**

Paper Code : ECMATH302 (A)

Optimization Techniques

Credits: 5, Full Marks: 70, Pass Marks: 28

Time: 3 hours

UNIT I – Dual Simplex Method

Infeasible optimal initial solution, Dual simplex method, Its advantage over simplex method, difference between simplex and dual simplex method. [2 QUESTIONS]

Lectures – 20

UNIT II – Sensitivity Analysis

Changes in coefficients in the objective function, Changes in the structure of the LPP due to addition of new variable/Deleting of existing variable/Addition of new constraints/Deletion of existing constraints. [2 QUESTIONS]

Lectures – 20

UNIT III – Theory of Games

Characteristics of game theory, maximin criteria and optimal strategy, solution of game with saddle points, Rectangular games without saddle points and its solutions by linear programming. [2 QUESTIONS]

Lectures–20

UNIT IV – Queuing Theory

Basic characteristics of queueing system, different performance measure, steady state solution of Markovian queueing models: M/M/1, M/M/1 with limited waiting space, M/M/C, M/M/C with limited waiting space.[2 QUESTIONS]

Lectures – 15

Text/ Reference Books:

1. S.D. Sharma, Operation Research, Kedar Nath, Ram Nath and Company (1972)
2. H.A. Taha, Operations Research, Prentice-Hall of India Private Limited (2003)
3. R.K. Gupta, Operations Research, Krishna Prakashan.

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Paper Code: ECMATH302 (B)

Advanced Discrete Mathematics

Credits: 5, Full Marks: 70, Pass Marks: 28

Time: 3 hours

UNIT I – Automata Theory

Lectures – 20

Finite state automata & types of automata, deterministic and non deterministic finite state automata, non deterministic finite state automata (NDFSA), transition diagram. Moore Machine, Mealy Machine Turing Machine.

[2 QUESTIONS]

UNIT II – Eulerian and Hamiltonian Graphs

Lectures – 20

Eulerian graph and its characterizations, Hamiltonian graph and sufficient conditions for a graph to be Hamiltonian.

[2 QUESTIONS]

UNIT III – Planar graph and vertex coloring of a graph

Lectures – 20

Planar graphs, Platonic graphs. Euler's theorem for planar graphs. Vertex coloring, chromatic number, chromatic polynomial, Brooks theorem, edge coloring, chromatic index, map coloring four color theorem.

[2 QUESTIONS]

UNIT IV – Algorithms in graph theory

Lectures – 15

NP – complete problems, greedy algorithms, connector problem and Kruskal's algorithm. Algorithms for Chinese postman problem. The Shortest path problem, Dijkstra's algorithm.

[2 QUESTIONS]

Text/ Reference Books:

1. R. J. Wilson, Introduction to Graph Theory, 5th ed., Addison Wesley, 2012.
2. John Clark and Derek Allan Holton, A first look at Graph Theory, World Sc., 1991
3. Narsingh Deo, Graph Theory, PHI New Delhi
4. Uday Singh Rajpoot, Advanced Discrete Mathematics, PHI (Eastern economic edition)

UNIVERSITY DEPARTMENT OF MATHEMATICS, N.P. UNIVERSITY
CBCS PATTERN SYLLABUS W.E.F. 2017-18

Paper Code: ECMATH302 (C)

Integral Transforms

Credits: 5, Full Marks: 70, Pass Marks: 28

Time: 3 hours

UNIT I – Laplace and Stieltjes Transforms

Lectures – 20

Laplace Transform : Definition and convergence theorems, Absolute convergence, Uniform Convergence, Complex inversion formula. Convolution theorem, Tauberian Theorems.

Stieltjes Transform : Definition and convergence theorem, Hardy and Littlewood theorem.

[2 QUESTIONS]

UNIT II – Fourier Transforms

Lectures – 20

Fourier Transform, Fourier Cosine Transform, Fourier Sine Transform, Conditions for existence of Fourier Transforms, Convolution Integral, Parseval's Theorem, Inversion Theorem.

[2 QUESTIONS]

UNIT III – Mellin Transform

Lectures – 20

Definition and elementary properties of Mellin transform, Mellin Transform of derivatives and integrals, The Mellin inversion theorem, Convolution theorems, solution of some integral equations via Mellin transform.

[2 QUESTIONS]

UNIT IV – Hankel Transform

Lectures – 15

Definition and elementary properties of Hankel Transform, Inversion theorem, Transform of elementary functions, Transform of derivatives of functions, Parseval relation, Relation between Fourier and Hankel transform.

[2 QUESTIONS]

Text/ Reference Books:

1. D. V. Widder, The Laplace Transform, Princeton Univ. Press.
2. Ian N. Sneddon, The use of integral Transforms, McGraw Hill.
3. Ian N. Sneddon, Fourier Transforms, Dover Publications, 2010
4. Loknath Debnath, Integral Transforms and their Applications, Chapman and Hall/CRC; 2nd ed., 2006
5. R. N. Bracewell, The Fourier Transform and its Applications, TMH, India.

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CBCS PATTERN SYLLABUS W.E.F. 2017-18

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MID SEMESTER EXAMINATION (MSE)

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END SEMESTER EXAMINATION (ESE)

A total of **EIGHT** questions will be set in which Question 1 will be **Short Answer Type** and **COMPULSORY**. Any **four** questions shall have to be answered by the examinees out of the remaining seven questions. The questions will be of equal marks and will be so framed that the students are able to answer them within the stipulated time.

ECMATH 303

Students should opt for anyone of the following

A. FLUID DYNAMICS

B. ANALYTICAL DYNAMICS AND CALCULUS OF VARIATIONS

C. PROBABILITY AND STATISTICS

Paper Code: ECMATH303 (A)

Fluid Dynamics

Credits: 5, Full Marks: 70, Pass Marks: 28

Time: 3 hours

UNIT I – Kinematics

Lectures – 20

Lagrangian and Eulerian methods, Equation of continuity in different coordinate systems, Boundary surfaces, Stream lines, Path lines and streak lines. Velocity potential, Irrotational and Rotational motions. vortex lines.[2 QUESTIONS]

UNIT II – Equations of Motion

Lectures – 20

Lagrange's and Euler's equations of motion. Bernoulli's theorem. Equation of motion by flux method. Impulsive actions. Stream function, Irrotational motion. [2 QUESTIONS]

UNIT III –

Lectures – 20

Complex velocity potential. Sources, sinks doublets and their images in two dimension. Conformal mapping. Milne-Thomson circle theorem. [2 QUESTIONS]

UNIT IV –

Lectures – 15

Two-dimensional Irrotational motion produced by motion of circular, co-axial and elliptic cylinders in an infinite mass of liquid. Theorem of Blasius. Motion of a sphere through a liquid at rest at infinity. Liquid streaming past a fixed sphere. Equation of motion of a sphere.[2 QUESTIONS]

Text/ Reference Books:

1. W.H. Besant, A. S. Ramsey. A Treatise on Hydro Mechanics. Part II. CBS Publ., 2006
2. G. K. Batchelor. An Introduction of Fluid Mechanics. Comb. Univ. Press, 2000.
3. F. Choriton. Textbook of Fluid Dynamics. C.B.S. Publishers. Delhi 1985
4. P. K. Bansal, A Text Book of Fluid mechanics, Laxmi Publ., 2008.
5. M. D. Raisinghani, Fluid dynamics, S Chand Publ.

UNIVERSITY DEPARTMENT OF MATHEMATICS, N.P. UNIVERSITY
CBCS PATTERN SYLLABUS W.E.F. 2017-18

Paper Code: ECMATH303 (B)

Analytical Dynamics and Calculus of Variations

Credits: 5, Full Marks: 70, Pass Marks: 28

Time: 3 hours

UNIT I – Lagrangian Dynamics

Lectures – 20

Generalized coordinates, Holonomic and Non-holonomic systems, Scleronomic and Rheonomic system, Generalized potential. Lagrange's equations of first and second kind, Energy equation for conservative fields.

[2 QUESTIONS]

UNIT II – Equations of Hamilton and Routh

Lectures – 20

Hamilton cononical equations. Equation of energy from Hamilton's equations, Cyclic coordinates, Routh's equations, Jacooi-Poisson Theorem.

[2 QUESTIONS]

UNIT III – Calcular of Variations

Lectures – 20

Motivating problems of calculus of variations fundamental lemma of calculus of variations Euler's equation, Brachistochrone problem Shortest distance, Geodesic, Minimum surface of revolution.

[2 QUESTIONS]

UNIT IV – Variational Principal in Dynamics and Brackets

Lectures – 15

Hamilton's Principle, Principle of least action. Jacobi's equations. Hamilton-Jacobi equations. Jacobi theorem. Lagrange brackets and Poisson brackets. Invariance of Langrange brackets and Poisson brackets under canonical transformations.

[2 QUESTIONS]

Text/ Reference Books:

1. H. Goldstein, Classical Mechanics (2nd edition), Narosa, Publishing House, New Delhi.
2. I. M. Gelfand and S.V. Fomin, Calculus of variation, prentice Hall.
3. S. L. Loney, An elementary treatise on Statics, Kalyani Publishers, N. Delhi 1979.
4. A. S. Ramsey, Newtonian Gravitation. The English Language Book Society and the Cambridge University Press.
5. N. C. Rana & P. S. Chandra Joag, Classical Mechanics. Tata McGraw Hill 1991
6. Lours N. Hand and Janel, D. Finch, Analytical Mechanics, Cambridge Univ. Press.

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CBCS PATTERN SYLLABUS W.E.F. 2017-18

Paper Code: ECMATH303 (C)

Probability and Statistics

Credits: 5, Full Marks: 70, Pass Marks: 28

Time: 3 hours

UNIT I –

Lectures – 20

Introduction to descriptive statistics and exploratory data analysis, sample space, discrete probability, independent events, Bayes theorem, random variables distribution functions, expectation and moments, marginal probability distribution, central limit theorem.

[2 QUESTIONS]

UNIT II –

Lectures – 20

Theoretical distributions, Standard discrete and continuous univariate distributions, Sampling distributions, standard errors such as statistical, biased or unbiased etc, Methods of estimation, Properties of estimators, Confidence intervals, Tests of hypothesis.

[2 QUESTIONS]

UNIT III –

Lectures – 20

Large sample tests, tests of single proportions, difference of proportions, tests of significance for single mean, difference of mean and difference of standard deviation. Chi-square distribution, goodness of fit, Chi-square test for independence of attributes, degree of freedom, population variance.

[2 QUESTIONS]

UNIT IV –

Lectures – 15

Tests of significance based on t, F and Z distributions.

[2 QUESTIONS]

Text/ Reference Books:

1. S. C. Gupta : Fundamentals of Statistics. Himalaya Publishing House, 1981.
2. Richard A. Johnson, Miller and Freunots : Probability and Statistics for Engineers.
3. B. Rosner : Fundamentals of Biostatistics, Duxbury Thompson Learning, 2000.

UNIVERSITY DEPARTMENT OF MATHETMATICS, N.P. UNIVERSITY
CBCS PATTERN SYLLABUS W.E.F. 2017-18



M.Sc./M.A. MATHEMATICS
SYLLABUS BASED ON CBCS SEMESTER SYSTEM
W. E. F. THE SESSION 2017-2018

SEMESTER IV

UNIVERSITY DEPARTMENT OF MATHEMATICS, N.P. UNIVERSITY
CBCS PATTERN SYLLABUS W.E.F. 2017-18

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MID SEMESTER EXAMINATION (MSE)

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END SEMESTER EXAMINATION (ESE)

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Paper Code: CCMATH409

Numerical Solution of ODE/PDE

Credits: 5, Full Marks: 70, Pass Marks: 28

Time: 3 hours

UNIT I – Numerical Solution of ODE-1

Lectures – 20

Picard's method of successive approximations for solution of first order ODE, Picard's method for simultaneous first ODE, Picard's method for second order ODE, Euler's method, Improved Euler's method, Modified Euler's method.

[2 QUESTIONS]

UNIT II – Numerical Solution of ODE-2

Lectures – 20

First order Runge-Kutta method, Runge-Kutta method of second order, Higher order Runge-Kutta methods, Runge-Kutta methods for simultaneous first order equations, Runge-Kutta method for second order ODE, Predictor-Corrector methods, Milne method, Adams-Bashforth method.

[2 QUESTIONS]

UNIT III – Numerical solutions of parabolic PDE

Lectures – 20

Numerical difference approximation of partial derivatives, Numerical solution of Heat equation, Two and three levels explicit and implicit difference schemes. Convergence and stability analysis.

[2 QUESTIONS]

UNIT IV – Numerical Solutions of Hyperbolic and Elliptic PDE

Lectures – 15

Numerical solution of hyperbolic PDE in one and two space dimension : explicit and implicit schemes. ADI methods. Difference schemes for first order equations. Numerical solutions of elliptic equations.

[2 QUESTIONS]

Text/ Reference Books:

1. M. K. Jain, S. R. K. Iyenger and R. K. Jain, Computational Methods for Partial differential equations, Wiley eastern, 1994.
2. M. K. Jain, Numerical solution of Differential Equations, second edition, Wiley Eastern.
3. Vadamurthy and Iyengar, Numerical methods, Vikas Publ., 2011.
4. V. Griffiths and I. M. Smith, Numerical Methods of Engineers, Oxford University Press. 1993.
5. F. General and P. O. Wheatley, Applied Numerical Analysis, Addison-Wesley, 1998.
6. K. E. Atkinson, An Introduction to Numerical Analysis, John Wiley & Sons.

UNIVERSITY DEPARTMENT OF MATHEMATICS, N.P. UNIVERSITY
CBCS PATTERN SYLLABUS W.E.F. 2017-18

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END SEMESTER EXAMINATION (ESE)

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Paper Code: ECMATH404

Students should opt for anyone of the following three courses:

- A. OPERATIONS RESEARCH**
- B. Fourier and Wavelet Analysis**
- C. MATHEMATICAL MODELING**

Paper Code: ECMATH404 (A)

Operation Research

Credits: 5, Full Marks: 70, Pass Marks: 28

Time: 3 hours

UNIT I – Integer Programming

Branch and bound technique, Gomory's cutting plane method.

Lectures – 20

[2 QUESTIONS]

UNIT II – Non Linear Programming

One and multi variable, Unconstrained optimization, Kuhn-Tucker Conditions for constrained optimization, Quadratic programming, Wolf's and Beal's method.

Lectures – 20

[2 QUESTIONS]

UNIT III – Inventory

Known demand, probabilistic demand, Deterministic Models and Probabilistic models without lead-time.

Lectures – 20

[2 QUESTIONS]

UNIT IV – Project Planning and Control with PERT-CPM

Rules of network construction, Time calculation in networks, Critical path method, PERT, PERT calculation, advantages of network (PERT/CPM), Difference between CPM and PERT.

Lectures – 15

[2 QUESTIONS]

Text/ Reference Books:

1. S. D. Sharma, Operation Research, Kedar Nath, Ram Nath and Company (1972).
2. H. A. Taha, Operations Research, PHI, 2003.
3. R. K. Gupta, Operations Research, Krishna Prakashan.

UNIVERSITY DEPARTMENT OF MATHEMATICS, N.P. UNIVERSITY
CBCS PATTERN SYLLABUS W.E.F. 2017-18

Paper Code: ECMATH404 (B)

Fourier and Wavelet Analysis

Credits: 5, Full Marks: 70, Pass Marks: 28

Time: 3 hours

UNIT I – Fourier series of periodic functions

Lectures – 20

Fourier Coefficients, partial sums, the Dirichlet and Fejer Kernels, convergence theorems. Fourier integrals : convolution, inversion, Plancherel's formula. Generalized Fourier Series, Orthogonality and completeness.

[2 QUESTIONS]

UNIT II – The Fourier Transform

Lectures – 20

basic properties, Inversion, Convolution, Plancherel Theorem, The Fourier Transform for L^2 functions, Dilatations, Translations, and Modulations. Windowed Fourier Transform, Discrete Fourier Transform.

[2 QUESTIONS]

UNIT III – Haar System and Haar Transform

Lectures – 20

The Haar System, Dyadic Step Functions, Haar bases on $[0, 1]$. Comparison of Haar series and Fourier Series. The Discrete Haar Transform (DHT), the DHT in two dimensions, Image analysis with the DHT.

[2 QUESTIONS]

UNIT IV – Orthonormal wavelet bases and Multiresolution analysis

Lectures – 15

Definition and examples, Constructin of Orthonormal wavelet bases, Scaling functions and their properties. The Discrete wavelet Transform, Wavelet frames, Multiscale Analysis, DWT for finite signals. The Continuous Wavelet Transform, Inverse CWT and admissibility conditions.

[2 QUESTIONS]

Text/ Reference Books:

1. D. F. Walnut, An Introduction to Wavelet Analysis, Birkhauser
 2. M. A. Pinsky, Introduction to Fourier Analysis and Wavelets, AMS.
 3. J. S. Walker, A Primer on Wavelets and Their Scientific Applications, CRC, 1999.
 4. R. M. Rao, A. S. Bopardikar, Wavelet Transforms, Pearsons, India, 2010.
 5. I. Daubechies, Ten Lectures on Wavelets, SIAM, 1992.
 6. Y. Meyer, Wavelets : Algorithms and Applications, SIAM, 1993.
 7. S. V. Narasinmhan et al, Introduction to Wavelet Transform, Narosa, India, 2012.
- A. K. Louis et al, Wavelets: Theory and Applications, John Wiley & Sons, 1998

UNIVERSITY DEPARTMENT OF MATHEMATICS, N.P. UNIVERSITY
CBCS PATTERN SYLLABUS W.E.F. 2017-18

Paper Code: CCMATH404 (C)

MATHEMATICAL MODELING

Credits: 5, Full Marks: 70, Pass Marks: 28

Time: 3 hours

UNIT I – Introduction to mathematical modeling

Lectures – 20

Simple situations requiring mathematical modeling, techniques of mathematical modeling, classifications, characteristics and limitations of mathematical models, some simple illustrations.

[2 QUESTIONS]

UNIT II – Mathematical modeling through differential equations

Lectures – 20

Linear growth and decay models, non linear growth and decay models, Compartment models, Mathematical modeling in dynamics through ordinary differential equations of first order.

[2 QUESTIONS]

UNIT III – Mathematical models through difference equations

Lectures – 20

Some simple mathematical models, basic theory of linear difference equations with constant coefficients.

[2 QUESTIONS]

UNIT IV – Application of mathematical modeling in economics, finance & genetics

Lectures – 15

Mathematical modeling through difference equations in economics and finance, mathematical modeling through difference equations in population dynamics and genetics.

[2 QUESTIONS]

Text/ Reference Books:

1. J. N. Kapur, Mathematica Modeling, Wiley Eastern.
2. D. N. Burghes, Mathematical modeling in social Management and Life Science, Ellie Herwood and John Wiley.
3. F. Charlton, Ordinary Differential and Difference Equations, Van Nostrand.

UNIVERSITY DEPARTMENT OF MATHEMATICS, N.P. UNIVERSITY
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END SEMESTER EXAMINATION (ESE)

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Paper Code: ECMATH405

Students should opt for anyone of the following three courses :

- A. INTEGRAL EQUATIONS
- B. HADAMARD MATRICES AND COMBINATORIAL DESIGNS
- C. MATHEMATICS OF FINANCE AND INSURANCE

Paper Code: ECMATH405 (A)

Integral Equations

Credits: 5, Full Marks: 70, Pass Marks: 28

Time: 3 hours

UNIT I – Classification of Linear Integral Equations

Fredholm, Volterra, Integro-Differential Equations, Singular Integral Equations, Converting Volterra Equation to ODE, Conversion of IVP to Volterra equation, Conversion of BVP to Fredholm equation.

Lectures – 20

[2 QUESTIONS]

UNIT II – Fredholm Integral Equations

Decomposition method, Direct Computation method, successive approximation method, method of successive substitutions, Homogeneous Fredholm Equations, Comparison between alternative methods.

Lectures – 20

[2 QUESTIONS]

UNIT III – Volterra Integral Equation

Solution of VIE, Series solution method, Successive Approximation method, Successive substitution method, Comparison between alternative methods. [2 QUESTIONS]

Lectures – 20

UNIT IV – Singular Integral Equations

Abel problem, Generalized Abel Integral Equation, Existence and uniqueness of solutions using fixed-point theorems in case of Linear and nonlinear Volterra and Fredholm integral equations. Solution of Integral equations by Laplace, Fourier transforms methods.[2 QUESTIONS]

Lectures – 15

Text/ Reference Books:

1. Murry R. Spiegel, Laplace Transform (SCHAUM Outline Series), McGraw-Hill.
2. Abdul J. Jerry, Introduction to integral equations with applications, Marcel Dekkar Inc. NY.
3. R. P. Kanwal, Linear Integral equations, Springer Sc., 1997
4. Harry Hochsdedt, Integral Equations, John Wiley & Sons.

UNIVERSITY DEPARTMENT OF MATHEMATICS, N.P. UNIVERSITY
CBCS PATTERN SYLLABUS W.E.F. 2017-18

Paper Code: ECMATH405 (B)

Hadamard Matrices and Combinatorial Designs

Credits: 5, Full Marks: 70, Pass Marks: 28

Time: 3 hours

UNIT I – Introduction to Hadamard Matrices

Lectures – 20

Order of Hadamard Matrix, Hadamard Matrix Conjecture, Kronecker Product of Hadamard Matrices, Sylvester Hadamard Matrices, Equivalence of Hadamard matrices, Maximum Determinant Theorem.

[2 QUESTIONS]

UNIT II – Construction of Hadamard Matrices

Lectures – 20

Hadamard matrices by Paley type I and type II methods, Williamson's method of construction. Number of inequivalent Hadamard matrices of order 16 & 20.

[2 QUESTIONS]

UNIT III – Orthogonal Designs

Lectures – 20

Orthogonal-design, weighing and Conference matrices, Baumert-Hall method for the construction of Hadamard matrices.

[2 QUESTIONS]

UNIT IV – Application of Hadamard Matrices

Lectures – 15

Construction of BIBD's from Hadamard matrices. Error correcting codes. Application of Hadamard matrices in the construction of error correcting codes.

[2 QUESTIONS]

Text/ Reference Books:

1. Marshall Hall (Jr.), Combinatorial Theory, Blaisdel Publishing house, 1986

UNIVERSITY DEPARTMENT OF MATHEMATICS, N.P. UNIVERSITY
CBCS PATTERN SYLLABUS W.E.F. 2017-18

Paper Code: ECMATH405 (C)

MATHEMATICS OF FINANCE AND INSURANCE

Credits: 5, Full Marks: 70, Pass Marks: 28

Time: 3 hours

UNIT I –

Lectures – 20

Financial Derivatives – An Introduction : Types of Financial Derivatives – Forwards and Futures : Options and its kind : and SWAPS.

The Arbitrage Theorem and Introduction to portfolio Selection and Capital Market Theory – Static and Continuous – Time Model.

[2 QUESTIONS]

UNIT II –

Lectures – 20

Pricing by Arbitrage – A single – Period Option Pricing Model :

Multi Pricing

Model – Cox – Rose – Rubinstein Model : Bounds on Option Prices.

The Dynamics of Derivative Prices – Stochastic Differential Equations (SDEs) – Major Models of SDEs. Linear Constant Coefficient SDEs : Geometric SDEs : Square Root Process : Mean Reverting Process and Ornstein – Uhlenbeck Process.

Martingale Measure and Risk-Neutral Probabilities : Pricing of Binomial Options with equivalent martingale measures.

[2 QUESTIONS]

UNIT III –

Lectures – 20

The Black-Scholes Option Pricing Model – Using no arbitrage approach, limiting case of Binomial Option Pricing and Risk – Neutral probabilities. The American Option Pricing – Extended Trading Strategies; Analysis of American Put Options : early exercise premium and relation to free boundary problems.

Concepts from Insurance : Introduction : The Claim Number Process : The Claim Size Process : Solvability of the Portfolio : Reinsurance and Ruin Problem. Premium and Ordering of Risks – Premium Calculation Principles and ordering Distributions.

[2 QUESTIONS]

UNIT IV –

Lectures – 15

Distributions of Aggregate Claim Amount – Individual and Collective Model : Compound Distributions : Claim Number of Distributions : Recursive Computation Methods : Lundberg Bounds and Approximation by Compound Distributions. Risk Processes – Time – Dependent Risk Models : Poisson Arrival Processes : Ruin Probabilities and Bounds Asymptotic and Approximation. Time Dependent Risk Models – Ruin Problems and Computations of Ruin Functions; Dual Queuing Model : Risk Models in Continuous Time and Numerical Evaluation of Ruin Functions.

[2 QUESTIONS]

Text/ Reference Books:

1. John C. Hull, Options, Futures and other derivatives. Prentice Hall of India Pvt. Ltd.
2. Sheldon M. Ross, // An Introduction to Mathematical Finance. Cambridge University Press.

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